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07 April 2016

Version of attached file:

Published Version

Peer-review status of attached file:

Peer-reviewed

Citation for published item:

Xie, L. and Guo, Q. and Cooper, A. P. and Frenk, C. S. and Li, R. and Gao, L. (2015) 'The size evolution of elliptical galaxies.', *Monthly notices of the Royal Astronomical Society.*, 447 (1). pp. 636-645.

Further information on publisher's website:

<http://dx.doi.org/10.1093/mnras/stu2487>

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The size evolution of elliptical galaxies

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Accepted 2014 November 24. Received 2014 November 24; in original form 2014 October 1

ABSTRACT

Recent work has suggested that the amplitude of the size–mass relation of massive early-type galaxies (ETGs) evolves with redshift. Here we use a semi-analytical galaxy formation model to study the size evolution of massive ETGs. We find this model is able to reproduce the amplitude and slope of the relation between size and stellar mass for these galaxies, as well as its evolution. The amplitude of this relation reflects the typical compactness of dark haloes at the time when most of the stars are formed. This link between size and star formation epoch is propagated in galaxy mergers. Mergers of high or moderate mass ratio (less than 1:3) become increasingly important with increasing present day stellar mass for galaxies more massive than $10^{11.4} M_{\odot}$. At lower masses, low mass ratio mergers play a more important role. In situ star formation contributes more to the size growth than it does to stellar mass growth. We also find that, for ETGs identified at $z = 2$, minor mergers dominate subsequent growth both for stellar mass and in size, consistent with earlier theoretical results.

Key words: methods: numerical – galaxies: evolution.

1 INTRODUCTION

The most massive galaxies are typically early-type galaxies (ETGs). Understanding the abundance and properties of ETGs is very important for galaxy formation theory and is also relevant to the determination of cosmological parameters (e.g. De Lucia & Blaizot 2007; Conselice 2014). The evolution of ETGs is thought to be driven by mergers, and hence to reflect the hierarchical nature of structure formation in the Λ cold dark matter (Λ CDM) model (Frenk et al. 1985; White & Frenk 1991; Kauffmann, White & Guiderdoni 1993; Lacey & Cole 1993; Parry, Eke & Frenk 2009).

Size is one of the most important observables in efforts to understand the evolution of ETGs. The size of a galaxy is typically defined as the projected radius, R_e , containing half of its stellar mass, M_* . The scaling relation between R_e and M_* for the ETG population has been studied by a number of recent galaxy surveys (e.g. Shen et al. 2003; Buitrago et al. 2008; Bernardi et al. 2010; Cooper et al. 2012; Cassata et al. 2013; van der Wel et al. 2014). It has been known for many years that ETGs (defined according to various combinations of mass, star formation rate, colour and surface brightness profile shape) are much more compact at high redshift, compared to their counterparts in the local Universe (Daddi et al. 2005; di Serego Alighieri et al. 2005; McIntosh et al. 2005; Trujillo et al. 2006). An often-quoted result is that the effective radius of a ‘typical massive ETG’ increases by up to a factor of ~ 4 from $z = 2.5$ to 0

(Trujillo et al. 2006; Buitrago et al. 2008; van Dokkum et al. 2008; Cenarro & Trujillo 2009; Cassata et al. 2011; Damjanov et al. 2011; van der Wel et al. 2014). Over the same redshift range, the corresponding ‘typical mass’ increases by only a factor of 2 (van Dokkum et al. 2010; Baldry et al. 2012). These results most often refer to the average size and mass of all ETGs above a fixed mass, applying the same rest-frame selection criteria at all redshifts. Recent work has provided more detailed insights: for example, there is evidence that the size increase may have been larger for galaxies of larger present-day stellar mass (Ryan et al. 2012), and Saracco, Longhetti & Gargiulo (2011), Shankar et al. (2013), Napolitano, Romanowsky & Tortora (2010) found that the size of ETGs selected may depend on their stellar age. This age dependence is not apparent in the local Universe (Trujillo, Ferreras & de La Rosa 2011). The central stellar mass density of massive galaxies at high redshift is similar to that of comparable galaxies in the local Universe (Bezanson et al. 2009; Hopkins et al. 2009; van Dokkum et al. 2010; Huang et al. 2013), and the majority of the evolution of the stellar mass density profiles of these galaxies seems to occur in their low surface brightness outer regions (Saracco, Gargiulo & Longhetti 2012). Similarly, the central velocity dispersion of ETGs shows only a weak decline with decreasing redshift at $z \lesssim 2$ (Cenarro & Trujillo 2009).

Explanations for these observations have been sought in the context of the Λ CDM model. This is far from straightforward – unlike the growth of dark matter structure, galaxy evolution in Λ CDM has a number of redshift-dependent characteristic scales introduced by baryonic physics (Guo & White 2008). Moreover, when galaxy populations are defined by redshift-independent selection functions

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(as in the case of ETGs), it becomes necessary to account for the apparent ‘evolution’ due to galaxies entering and leaving these selections, in addition to the evolution of galaxies that remain in the sample from high to low redshift. A fully self-consistent theory of how the ETG population evolves therefore requires a complete forward model of the entire galaxy population.

Here we study the size–mass relation of the ETG population at different epochs, from $z \sim 2$ to 0, in the semi-analytic galaxy formation model developed by Guo et al. (2011, 2013). This model reproduces many properties of galaxies observed in the local Universe and at high redshift, including the size–mass relation for both early- and late-type galaxies at the present day (Guo et al. 2011). We compare our model to observed galaxy size data over the same redshift range. In the context of the evolving amplitude of the size–mass relation, we examine the origin and relative importance of sample evolution and intrinsic evolution, concentrating on the mechanisms naturally provided by standard galaxy formation theory, namely star formation and dissipationless merging.

Mergers of high mass ratio, in particular, are thought to be capable of increasing galaxy size while providing relatively little corresponding increase in mass and having little or no effect on central density or velocity dispersion (Cole et al. 2000; Bezanson et al. 2009; Hopkins et al. 2009; Trujillo et al. 2011; Newman et al. 2012; Hilz, Naab & Ostriker 2013). Evolution dominated by these ‘minor’ mergers therefore provides a plausible explanation of the observational results at $z \lesssim 2$ mentioned above [$\delta R_e \propto (\delta M_*)^2$; e.g. Naab, Johansson & Ostriker 2009]. Observational arguments supporting this hypothesis have also been made based on the greater frequency of higher mass ratio mergers (e.g. McLure et al. 2013; Trujillo 2013). Recent hydrodynamical simulations (e.g. Naab et al. 2009; Oser et al. 2012) and N -body experiments (Laporte et al. 2013) have demonstrated that this explanation is indeed plausible in a cosmological context. In our model, the various evolutionary processes relevant to ETGs are included consistently with one another and with the galaxy population as a whole, allowing us to comment further on the relative importance of minor mergers. Note we do not address the nature of so-called ultracompact galaxies, which represent a small fraction of the $z \sim 2$ ETG population and are thought to form through intense, highly dissipative starbursts (e.g. Dekel et al. 2009; Hopkins et al. 2009).

This paper is structured as follows. In Section 2 we briefly describe the N -body simulation and semi-analytic model used for this work. In Section 3 we compare size–mass relations at different redshifts in the model to observed relations. In Section 4 we study the different mechanisms driving the evolution of the size–stellar mass relation in the model. We summarize our results in Section 5.

2 SIMULATION AND SEMI-ANALYTICAL MODELS

The galaxy formation model in this work is based on dark matter halo merger trees extracted from the cosmological N -body *Millennium Simulation*. Descriptions of the *Millennium Simulation* and our galaxy formation model can be found in Springel et al. (2005) and Guo et al. (2011, 2013), respectively. Here we summarize the most important characteristics of the simulation and the equations in the model relevant to the sizes of ETGs.

2.1 The simulation

The *Millennium Simulation* (Springel et al. 2005) is a cosmological N -body simulation, which follows 2160^3 particles from

redshift $z = 127$ to the present day in a box of length $500 \text{ Mpc } h^{-1}$ on each side (where the Hubble parameter $h = 0.73$). This volume is large enough to investigate the statistical distributions of the properties of massive ETGs. Each dark matter particle has a mass of $8.6 \times 10^8 \text{ M}_\odot h^{-1}$, allowing us to follow galaxies down to masses comparable to that of the Small Magellanic Cloud. The simulation adopted cosmological parameters consistent with the first year *Wilkinson Microwave Anisotropy Probe* (WMAP) results: $\Omega_m = 0.25$, $\Omega_b = 0.045$, $\Omega_\Lambda = 0.75$, $\sigma_8 = 0.9$, $n = 1$.

Particle data were stored at 64 logarithmically spaced output times. At each snapshot, the friends-of-friends (FOF) group-finding algorithm was used to link particles separated by less than 0.2 of the average interparticle separation (Davis et al. 1985). The SUBFIND algorithm (Springel et al. 2001) was then applied to decompose these groups into self-bound substructures (hereafter subhaloes). Merger trees were constructed by linking subhaloes at different output times into chains of progenitors and descendants using the algorithm described in Springel et al. (2005) and Boylan-Kolchin et al. (2009). The galaxy model then processes these merger trees.

We call the most massive subhalo in a FOF group the ‘main halo’. A galaxy assigned to the potential minimum of a main halo is referred to as a central galaxy, while galaxies assigned to satellite subhaloes are referred to as satellite galaxies. Satellite galaxies include so-called ‘orphans’ whose subhaloes cannot be resolved anymore by the N -body simulation; the orbits of these galaxies are tracked semi-analytically, such that the ability to follow satellites until they merge is not limited by the resolution of the N -body simulation (Springel et al. 2001). For the main halo of each FOF group, we define a total mass, M_{200} , enclosed by a radius, R_{200} , within which the mean density is 200 times the critical density for closure at the corresponding redshift.

2.2 Semi-analytical model

In the standard Λ CDM model, galaxies grow in dark-matter-dominated potentials as the result of in situ star formation in condensed gas and the accretion of less massive satellite galaxies (White & Rees 1978). In contrast to the self-similar growth of dark matter haloes, the rate of change of stellar mass through both of these channels varies according to the existing stellar mass and, at a fixed mass, with redshift (Guo & White 2008). In this model, star formation always dominates the growth of stellar mass for low-mass galaxies (present-day $M_* \lesssim 10^{10} \text{ M}_\odot$). More massive galaxies grow mainly through star formation at $z \gtrsim 2$ and by accretion and merging thereafter. Detailed descriptions of stellar mass growth in similar galaxy formation models can be found in Guo et al. (2011, 2013), De Lucia & Blaizot (2007), Croton et al. (2006) and Springel et al. (2001). This model also tracks changes in the size of galaxies as their mass evolves. Galaxies are separated into three components – gas discs, stellar discs and stellar bulges. The size and mass of each of these components are followed separately, according to the following prescriptions.

2.2.1 Disc sizes

When gas condenses into the centre of a potential well, we assume that it has the same specific angular momentum ($j_{\text{gas,cooling}}$) as its host halo. The total angular momentum of the gas disc is thus

$$J_{\text{gas,new}} = J_{\text{gas,old}} + J_{\text{gas,cooling}} - J_{\text{gas,SF}} + J_{\text{gas,merger}}, \quad (1)$$

where $J_{\text{gas,new}}$ and $J_{\text{gas,old}}$ are the new and original total angular momentum of the gas disc, respectively. $J_{\text{gas,cooling}}$ is the total angular momentum of recently cooled gas ($J_{\text{gas,cooling}} = m_{\text{gas,cooling}} j_{\text{gas,cooling}}$, where $m_{\text{gas,cooling}}$ is the amount of gas cooled in a given time interval) and $J_{\text{gas,merger}}$ is the total angular momentum carried by the gas component of merging satellites. $J_{\text{gas,SF}}$ is the angular momentum lost to stellar disc through star formation.

The stellar disc gains angular momentum through star formation and loses it through disc instabilities, which transfer stars from the disc to the bulge component as required to marginally stabilize the stellar disc against gravitational instability. The balance equation for the stellar disc angular momentum is therefore

$$J_{\star,\text{new}} = J_{\star,\text{old}} + J_{\star,\text{SF}} - J_{\star,\text{instability}}, \quad (2)$$

where

$$J_{\star,\text{SF}} = J_{\text{gas,SF}} = M_{\star,\text{SF}} j_{\text{gas}}. \quad (3)$$

Here $M_{\star,\text{SF}}$ is the amount of new formed star and j_{gas} is the specific angular momentum of the gas disc.

We assume both the gas disc and the stellar disc have exponential surface density profiles and the circular velocity curve is flat, hence the exponential scale length of the gas or stellar disc is given by (Croton et al. 2006)

$$R_{\text{gas},\star} = \frac{J_{\text{gas},\star}/M_{\text{gas},\star}}{2V_{\text{cir}}}. \quad (4)$$

This equation is theoretical prediction Barnes 1984; Blumenthal et al. 1986. Here $M_{\text{gas},\star}$ denotes the total mass in the gas or stellar disc and $J_{\text{gas},\star}$ the corresponding total angular momentum. In practice we use V_{max} , the maximum circular velocity of the dark halo, as a proxy for V_{cir} . Note this directly connects the sizes of discs to the characteristic scale of their dark matter halo.

2.2.2 Spheroid sizes

When haloes become subhaloes of more massive systems, their galaxies become satellites. Satellites with resolved subhaloes survive until either (i) they are deemed to be tidally disrupted or (ii) their corresponding subhalo is lost from the N -body simulation and the time for their inspiral to the centre of their host potential is less than the lookback time at which their subhalo was lost. Further caveats to these prescriptions are described in Guo et al. (2011). Stars from tidally disrupted objects are placed into a ‘stellar halo’ reservoir. For the purposes of this paper, these stars are considered to be unobservable, and they are never transferred back to any central galaxy. Hence only stars from satellites merging to the centre of their host can influence the size of the host’s central galaxy.

Binary mergers between galaxies (and dark matter haloes) are often divided into ‘major’ and ‘minor’ categories according to mass ratio of the two progenitors. Following convention in the literature, Guo et al. (2011) used a baryon mass ratio threshold of 3: 1 to divide ‘major’ and ‘minor’ mergers. In this model of major mergers, violent relaxation leads to the complete destruction of centrifugally supported discs, such that the remnant is purely dispersion supported (e.g. Naab et al. 2007). In contrast, the disc of the more massive (primary) progenitor is allowed to survive in minor mergers, with the stars from the less massive (secondary) progenitor being scattered into the stellar spheroid (bulge) of the remnant. Note that 3: 1 is a rough value to distinguish major and minor mergers. This ratio is first used in Kauffmann et al. (1999) motivated by a series of N -body simulations of merging disc galaxies. We have repeated our analysis using mass ratio of 10: 1 to test how this choice affects our

result. We found that the fraction of elliptical galaxies in the mass range we consider are almost the same, but their sizes are about 10 per cent larger. However the slope of the size–mass relation is the same. We believe that our results are not sensitive to the exact value of this threshold.

Mergers also trigger rapid gas dissipation, represented by a ‘starburst’ mode of star formation. In the case of major mergers, all gas from both progenitors is used to fuel a starburst that adds stars to the spheroidal component of the remnant. In the minor merger case, gas from the secondary progenitor is added to the gas disc of the remnant, and stars formed in the starburst are also added to the surviving stellar disc. These bursts can convert a large fraction of the available cold gas into stars. A recipe from Somerville, Primack & Faber (2001) is used here to model the fraction of gas converted into stars during a starburst:

$$\epsilon_{\text{burst}} = 0.56 \left(\frac{M_{\text{sat}}}{M_{\text{cen}}} \right)^{0.7}, \quad (5)$$

where M_{sat} and M_{cen} are the total baryonic mass of the satellite and central galaxies, respectively. The parameter values here are derived from fits to the results of hydrodynamical simulations (Mihos & Hernquist 1994, 1996).

Assuming energy conservation and virial equilibrium, the growth in the size of the spheroid component in a merger between two galaxies can be approximated by (Cole et al. 2000)

$$C \frac{GM_{\text{new,b}}^2}{R_{\text{new,b}}} = C \frac{GM_{\text{sat}}^2}{R_{\text{sat}}} + C \frac{GM_{\text{cen}}^2}{R_{\text{cen}}} + \alpha \frac{GM_{\text{sat}}M_{\text{cen}}}{R_{\text{sat}} + R_{\text{cen}}}. \quad (6)$$

Here C is the so-called structure parameter, relating the binding energy of a galaxy to its mass and radius. Formally, it is 0.49 for exponential disc galaxies, and 0.45 for spheroids with an $r^{-1/4}$ density profile. Here C , as in Guo et al. (2011), we adopt a compromise value of 0.5 for all galaxies. The factor α parametrizes the effective interaction energy of the two galaxies. Shankar et al. (2014) found that the slope of the bulge size versus stellar mass relation depends strongly on this quantity. Guo et al. (2011) adopted $\alpha = 0.5$ in order to reproduce the observed bulge size versus stellar mass relation for ellipticals (Shen et al. 2003). This particular value is also roughly consistent with the numerical simulation results given by Boylan-Kolchin, Ma & Quataert (2005), for typical orbits of dissipationless major mergers.

In major mergers, both existing stars and stars formed in the associated starburst are counted when calculating the spheroid size of the remnant, i.e. $M_{\text{cen/sat}} = M_{\text{cen/sat},\star} + \epsilon_{\text{burst}} M_{\text{cen/sat,gas}}$, where $M_{\text{cen/sat},\star}$ and $M_{\text{cen/sat,gas}}$ are the stellar mass and cold gas mass of the central and satellite galaxies, respectively. In minor mergers, all stars in the satellite galaxy are added to the bulge of the central galaxy. The corresponding M_{cen} and M_{sat} are then assumed to be $M_{\text{cen,b}}$ and $M_{\text{sat},\star}$, respectively, where $M_{\text{cen,b}}$ denotes the stellar mass in the spheroids of the central galaxies. R_{sat} and R_{cen} are the corresponding half-mass radii.

Dynamical instabilities in the disc are another important channel by which stars are transferred to the spheroidal component. Guo et al. (2011) assumed a simple criterion to estimate the onset of instability:

$$V_{\text{max}} < \sqrt{\frac{GM_{\text{disc},\star}}{3R_{\text{disc},\star}}}, \quad (7)$$

where $M_{\text{disc},\star}$ is the mass of the stellar disc and $R_{\text{disc},\star}$ its exponential scale length. When equation (7) is satisfied, a stellar mass of δM_{\star} is transferred from the disc to the spheroid such that the disc is

made marginally stable. The corresponding growth in spheroid size is also modelled using equation (6), defining M_{cen} and R_{cen} to be the stellar mass and the half-mass radius of the existing bulge, if any, and $M_{\text{sat}} = \delta M_*$ and R_{sat} to be the radius containing a mass δM_* in the unstable disc. The pre-factor α is set to 2 in this case, higher than in the merger case, since the ‘old’ and ‘new’ spheroid stars at least partly overlap at the onset of the instability, implying a higher interaction energy.

Although the Guo et al. (2011) model accounts for the rapid conversion of gas dissipated in mergers to stars, the energy balance represented by equation (6) does not take this dissipation into account. Doing so would reduce the size of the remnant further in cases where gas makes up a substantial fraction of the mass of either progenitor (e.g. Covington et al. 2008). Shankar et al. (2013) have shown that the sizes of low-mass ETGs in this model would be in better agreement with observations if this effect was included. Such changes are beyond the scope of the present paper.

2.3 Projected half-mass radius

All the radii discussed above are defined in three dimensions. To compare these to observational data directly, we need to convert them to radii in projection. We assume that the spheroidal components of our galaxies follow a Jaffe profile (Jaffe 1983):

$$j_b = \frac{M_b r_b}{4\pi r^2 (r + r_b)^2}. \quad (8)$$

Here M_b is the stellar mass of the bulge, and r_b is the corresponding 3D half-mass radius. The projected density profile is given by

$$I_b(R) = \int_R^\infty j(r) \frac{r}{(r^2 - R^2)^{1/2}} dr. \quad (9)$$

We assume the Jaffe model to simplify this calculation, noting that it may not be a good description of all galactic spheroids.

We assume an exponential profile for the disc component:

$$I_d = \frac{M_d}{2\pi r_d^2} e^{-r/r_d}, \quad (10)$$

where M_d is the stellar mass of the disc and r_d the exponential scale length. The total surface mass density (surface brightness) is the sum of these two components:

$$I(r) = I_b(r) + I_d(r). \quad (11)$$

2.4 Fiducial ETG definition

A wide variety of definitions of the ETG population are found in the literature. Some specify the fraction of light or mass in the spheroidal component, some impose upper limits on specific star formation rate (sSFR) and some select by colour or spectral shape. To perform a meaningful comparison between model predictions and observational data in the following section, we will adapt our selection criteria to match roughly those of each data set we compare to. For simplicity, however, in all other sections this paper we use only one fiducial classification of ETGs in the model, according to their total stellar mass, bulge-to-total stellar mass ratio and sSFR:

$$M_* > 1 \times 10^{11} M_\odot, \quad M_b/M_* > 0.9, \quad \text{sSFR} < 10^{-11} \text{ yr}^{-1}. \quad (12)$$

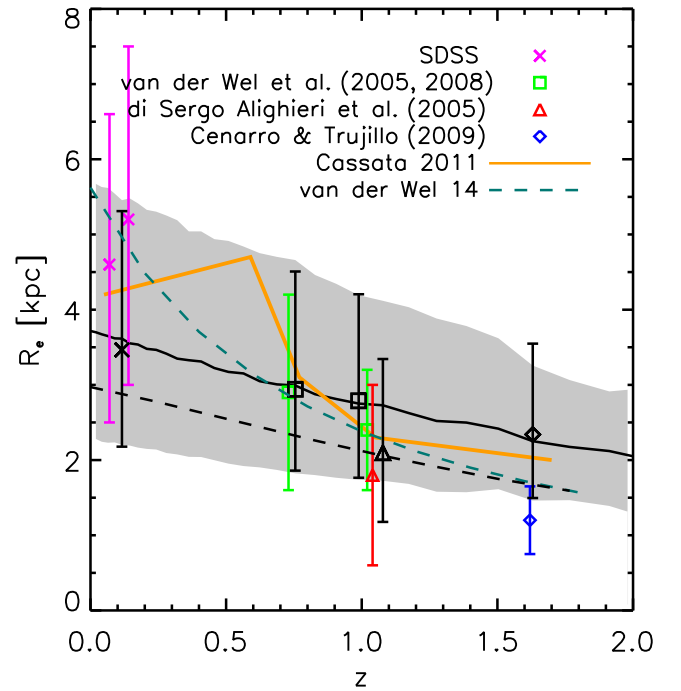


Figure 1. Projected half-mass radius as a function of redshift. Black curves and symbols are the model predictions, while coloured curves and symbols with error bars are the measurements in the literature. Different observations use somehow different selection criteria for ETGs. Detailed selection criteria can be found in Table 1. Solid, dashed curves and symbols denote the median values of the corresponding size distribution. Errors along the y-axis and the shaded region represent 16–84 per cent ranges.

3 SIZE EVOLUTION

3.1 Model versus observation

In this section, we compare the evolution of the size of ‘typical’ ETGs and the entire ETG size–mass relation between model predictions and observations.

Fig. 1 shows how the median size of the ETG population in the model, defined according to our fiducial criterion (equation 12), varies with redshift (solid black line). The median size of galaxies selected in this way increases by a factor of ~ 1.8 between redshift $z \sim 2$ and 0.

We compare this prediction with a number of recent observational estimates obtained at different redshifts. For each coloured point or line in Fig. 1, representing an observational result, there is a corresponding black point or line of the same style representing an equivalent selection from the model. The data sets and selection criteria are summarized in Table 1. To reflect uncertainties in the observational determination of stellar mass (Longhetti & Saracco 2009; Mitchell et al. 2013), we have convolved the stellar mass of each model galaxy with a Gaussian of dispersion 0.25 dex in $\log_{10} M_*$. Where necessary, we have recalibrated stellar masses from observations to the assumption of a universal Chabrier initial mass function (IMF; Chabrier 2003) used by Guo et al. (2011).

The median size of model ETGs at $z = 0$ is ~ 1 kpc lower than the Sloan Digital Sky Survey (SDSS) data quoted by Cassata et al. (2011) (yellow line). At $z \sim 1$, ETGs in the model have very similar sizes to their counterparts in observations, either selected by morphology (van der Wel et al. 2005, 2008) (green squares) or spectral

Table 1. A summary of the observational data we compare to the model. From left to right, columns are as follows: (1) observational data source (as Fig. 1); (2) the survey or catalogue from which the data originate; (3–6) respectively mass, morphology, sSFR and redshift criteria that define each sample, in the observational data and the corresponding model selection; (7) the symbol/line style and colour denoting the data and its model comparison in Fig. 1. Note that morphological criteria are most difficult to match with the model. When selecting ETGs’ morphology, Cassata et al. (2011) and van der Wel et al. (2005, 2008) selected visually spheroidal galaxies; Cenarro & Trujillo (2009) selected galaxies with Sérsic index $n > 2.5$ and di Serego Alighieri et al. (2005) and van der Wel et al. (2014) did not set limitations on morphology or sSFR, but instead selected galaxies by an early-type spectral classification and colour, respectively.

Former works (1)	Surveys (2)	M_* ($10^{11} M_\odot$) (3)	Morphology (4)	sSFR (10^{-11} yr^{-1}) (5)	z (6)	Symbol/line (7)
Cassata et al. (2011) model	GOODS WFC3	$M_* > 1$ $M_{\text{star}} > 1$	Visually spheroidal $M_b/M_* > 0.9$	sSFR < 1 sSFR < 1	$0 < z < 2.5$ $0 < z < 2.0$	Yellow line Black line
Cenarro & Trujillo (2009) model	SDSS DR6	$0.5 < M_* < 2$ $0.5 < M_* < 2$	S0, E $M_b/M_* > 0.9$		$0 < z < 0.1$ $z \sim 0.12$	Purple crosses Black cross
Cenarro & Trujillo (2009) model	GMASS	$0.5 < M_* < 2$ $0.5 < M_* < 2$	S0, E $M_b/M_* > 0.9$		$1.4 < z < 2.0$ $z \sim 1.63$	Blue diamond Black diamond
van der Wel et al. (2005) model	CDFS, RDCS	$0.5 < M_* < 2$ $0.5 < M_* < 2$	S0, E $M_b/M_* > 0.9$		$0.9 < z < 1.2$ $z \sim 0.99$	Green squares Black square
van der Wel et al. (2008) model	CDFS, RDCS	$0.5 < M_* < 2$ $0.5 < M_* < 2$	S0, E $M_b/M_* > 0.9$		$0.6 < z < 0.8$ $z \sim 0.76$	Green squares Black square
di Serego Alighieri et al. (2005) model	K20	$0.5 < M_* < 2$ $0.5 < M_* < 2$		Early-type spectrum sSFR < 1	$0.88 < z < 1.3$ $z \sim 1.1$	Red triangle Black triangle
van der Wel et al. (2014) model	3D-HST, CANDELS	$0.3 < M_* < 1$ $0.3 < M_* > 1$		$U - V, V - J$ sSFR < 1	$0 < z < 2$ $0 < z < 2$	Cyan dashed curve Black dashed lines

energy distribution (di Serego Alighieri et al. 2005) (red triangles). For ETGs selected by both morphology and sSFR (Cassata et al. 2011), the model predictions are consistent with the observed results at the 1σ level up to redshift $z \sim 1.5$.

In the study of van der Wel et al. (2014) (cyan dashed curve), ETGs were selected by colour – we used sSFR as a proxy for this selection as colours in the model are subject to additional uncertainties. The discrepancy between the model and these observations decreases at higher redshift. Samples drawn from the model with the mass and morphology criteria of Cenarro & Trujillo (2009) (yellow line) lie on the line defined by our fiducial selection, because the morphology cut is the same and the mass cut makes no practical difference. However, the data of Cenarro & Trujillo (2009) define a significantly steeper relation, with a larger median size compared to the model at low redshift and slightly smaller median size compared to the model at $z = 2$.

Although there is some tension between the model and data at high and low redshift, the trend of size evolution of the model from $z = 2$ to the present day is in reasonable agreement with observations. ETG samples have a smaller median size at $z \sim 2$ by a factor of ~ 1.8 . We note that, since the mass range defining ETGs is only bounded at low mass, the fact that more high-mass ETGs enter the sample at low redshift would cause some evolution in the ‘average’ size of the ETG population even if the amplitude and slope of the size–mass relation remained fixed. However, as the galaxy mass function truncates exponentially at high masses, the contribution of additional high-mass galaxies to the average size measure is only of the order of a few per cent. Hence, the increase in average size must be driven by a change in the overall amplitude of the size–mass relation with redshift.

In Fig. 2 we compare the evolution of the model size versus stellar mass relation with observations in three redshift intervals. Red circles in each panel show measurements by Williams et al. (2010), who used SDSS data at $z \approx 0$ and an updated version of the K -selected galaxy catalogue of Williams et al. (2009) for higher redshift galaxies. ETGs are defined by $\text{sSFR} < 0.3/t_H$, where t_H is

the age of the Universe at the corresponding redshift. We select model ETGs with the same criteria; the red solid curve with errors indicates their median size and its 1σ deviation, respectively. Note that instead of including all galaxies in the same redshift intervals of Williams et al. (2010), we select only in a narrow slice around the median redshift of each interval. For a given stellar mass, the half-mass radius of ETGs selected in this way is predicted to increase by a factor of 1.6 across this range of redshift – this change in amplitude is substantially greater than the increase in the ‘typical’ mass of ETGs due to the inclusion of a larger fraction of very massive galaxies at low redshift. Model predictions are broadly consistent with the Williams et al. (2010) data at all redshifts, particularly for high-mass ETGs. The agreement for low-mass ETGs is somewhat better at higher redshift.

Most recently, Cassata et al. (2013) used the Cosmic Assembly Near-Infrared Deep Extragalactic Legacy Survey (CANDELS) to study the size versus stellar mass relation for ETGs between $1 < z < 3$. They selected spheroidal galaxies with $10^{10} < M_\odot < 10^{11.5} M_\odot$ and $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$. Individual measurements for each of their galaxies are shown with green symbols in Fig. 2. For comparison we select model galaxies with $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$ and $M_{\text{bulge}}/M_{\text{star}} > 0.9$. The size–mass relations of this selection at the median redshift of each interval explored by Cassata et al. (2013) are shown with green solid curves (1σ errors). Model predictions for ETGs selected in this way are less obviously consistent with the observational data than in the previous case, particularly in the highest redshift interval where the overestimate of size at low mass is even more pronounced. We believe this is (at least partly) because the Guo et al. (2011) model does not take into account dissipation of energy by gas during mergers. This should make the remnants of gas-rich high-redshift major mergers considerably smaller, but will not affect the remnants of gas-poor mergers, which dominate at lower redshift.

In summary, the evolution in the ‘typical ETG’ size in the model is driven primarily by the increasing amplitude of the size–mass relation with redshift.

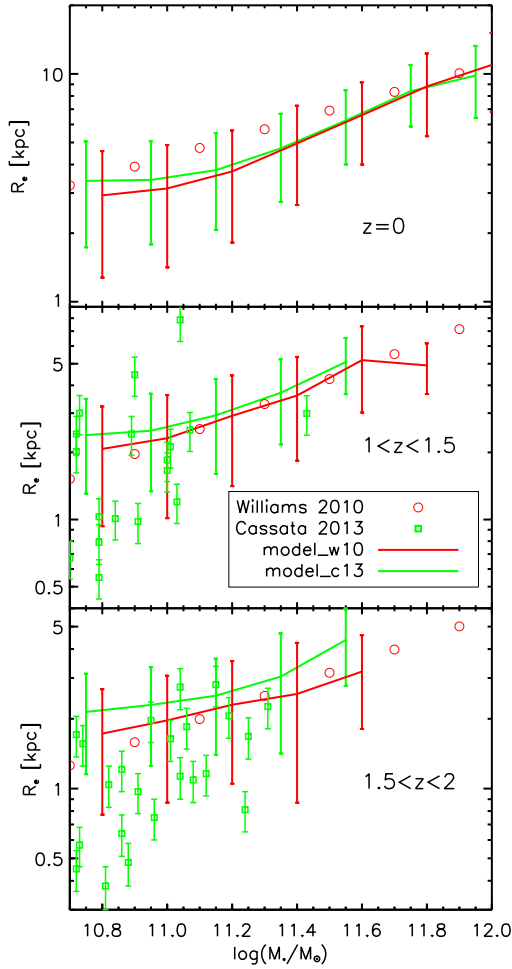


Figure 2. The size–stellar mass relation for ETGs selected at different redshifts. Red circles (Williams et al. 2010) and green squares (Cassata et al. 2013) are observational results in different redshift intervals, as indicated in each panel. Red and Green curves are the corresponding model predictions, with equivalent selections as described in the text. Error bars show the 1σ dispersion. Model galaxies are selected at the median redshift of each redshift interval of the corresponding observations, not over the entire redshift interval.

3.2 Amplitude of the size–mass relation

In this section, we will explore the origin of the evolution in the amplitude of the ETG size–mass relation. Two factors are relevant. First, galaxies classified as ETGs at high redshift can grow in mass and size over time. The size–mass relation will evolve according to the rate of size change per unit additional mass. Secondly, galaxies may enter (or leave) the ETG population. If the median size at fixed mass for ‘newly formed’ ETGs changes over time, the size–mass relation will evolve even if individual ETGs do not. Since the number of galaxies classified as ETGs at high redshift is only a few per cent of that at $z = 0$, the latter effect could easily dominate the apparent evolution in the observed size–mass relation.

To separate these two effects in the model, we divide ETGs into three disjoint sets, according to the redshift interval in which they are first identified as ETGs according to our fiducial selection.

- (i) *HighZ*: first identified as ETGs before $z = 1.6$.
- (ii) *MidZ*: first identified as ETGs in the range $1 < z < 1.6$.
- (iii) *LowZ*: first identified as ETGs after $z = 1$.

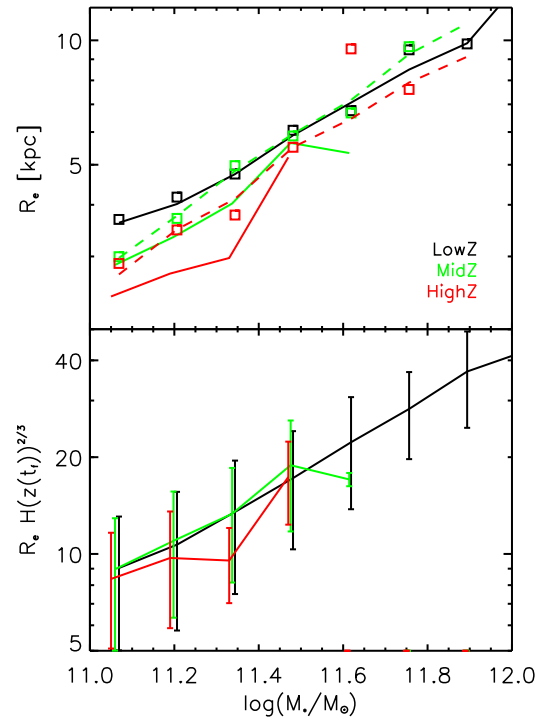


Figure 3. Top panel: size–mass relation of ETG samples identified at different redshifts. Solid lines show the median values of our *LowZ*, *MidZ* and *HighZ* samples. Dashed lines show the relation at $z = 0$ for descendants of the *MidZ* and *HighZ* samples. Open squares show the relation defined by satellites at $z = 0$ (using descendants of the *MidZ* and *HighZ* samples). Bottom panel: the mean size–mass relation for the three samples after rescaling by their star formation time, as described in the text. Error bars show the standard error of the mean size.

The top panel of Fig. 3 shows the median size–mass relation for each of these groups (red, green and black solid lines as indicated in the legend). The slope of the relation is almost independent of redshift. The amplitude increases by a factor of ~ 1.2 between successive groups. A dashed line of the same colour shows the relation defined by descendants of the corresponding group at $z = 0$ (almost all descendants are still ETGs). Descendants of the *HighZ* and *MidZ* samples cover the full mass range of the *LowZ* sample, showing that some galaxies have grown in mass. *HighZ* galaxies remain slightly more compact than more recently formed ETGs at a fixed mass. This may also be true for *MidZ* galaxies with descendants less massive than $2 \times 10^{11} M_{\odot}$.

Open square symbols in the top panel of Fig. 3 also show relations for the descendants of each sample at $z = 0$, but unlike the dashed lines they only include descendants that are satellites at $z = 0$. About 21 per cent of *HighZ* samples at $z = 0$ are satellites. The fraction is 27 per cent for *MidZ* samples. It can be seen that the relations for *HighZ* and *MidZ* are the same regardless of whether the galaxies have become satellites or not. This is consistent with the finding of Cassata et al. (2011) that, among galaxies in clusters, older galaxies have smaller sizes at given stellar mass. We predict that this is true also in the field.

At a fixed mass, dark matter haloes are more compact at high redshift, with the virial radius evolving as $R_{200}(z) \propto H(z)^{-2/3}$, where $H(z)$ is the Hubble parameter. In the model this redshift dependence of halo scale propagates to the sizes of newly formed galaxies, via the angular momentum conservation of infalling gas (equation 4).

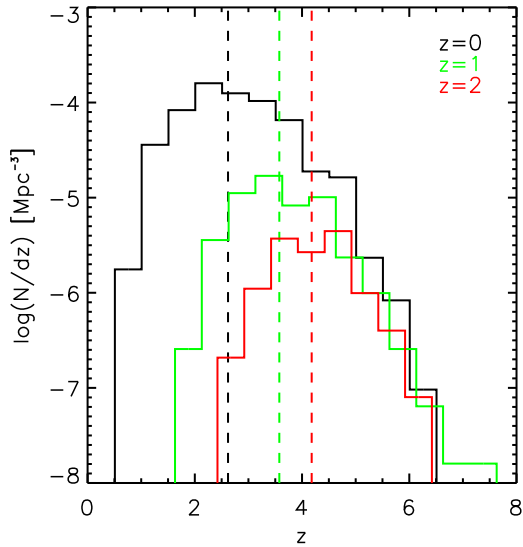


Figure 4. Distribution of the star formation time of our *LowZ*, *MidZ* and *HighZ* ETG samples, further restricted to have $10^{11} < M_{\star} < 3 \times 10^{11} M_{\odot}$. The colours of the three histograms correspond to those in Fig. 3. Dashed vertical lines indicate the corresponding median redshift of each sample.

The formation of bulges preserves the relative compactness of the system if the two progenitors are of similar age (hence size), but mergers with many more diffuse galaxies will have a ‘diluting’ effect (equation 6). Therefore, if galaxies form most of their stars at one early epoch, their sizes should reflect the initial scale of their host haloes even at $z = 0$, provided that their final mass is not dominated by mergers with galaxies formed at lower redshift.

To test this idea, we define a galaxy’s formation time t_f to be the time by which half of its $z = 0$ stellar mass is formed. Note that this is *not* time by which half the stellar mass is assembled into a single object (often used as a definition of galaxy ‘formation time’ in the literature). At t_f , the stars in one $z = 0$ galaxy may belong to many separate galaxies. Fig. 4 shows the distribution of t_f for *LowZ*, *MidZ* and *HighZ* are shown with black, red and green histograms, respectively. The formation time depends on stellar mass. Stars in massive ETGs assemble at earlier time than those in less massive ETGs. To remove the mass dependence, we further restrict to those with stellar mass $10^{11} < M_{\text{star}} < 3 \times 10^{11} M_{\odot}$. Dashed vertical lines of the same colour indicate the median formation redshift of the corresponding sample. For *LowZ*, the median redshift is 2.6, while for *HighZ* the median redshift is 4.2. The $H(z)^{-2/3}$ scaling between these two median redshifts predicts a factor of 1.4 difference in size, close to actual the difference between the *LowZ* and *HighZ* samples.

To illustrate this effect, we scale the radius of each galaxy by a factor of $H(z(t_f))^{2/3}$ and recompute the size–mass relation for each sample. The results are shown in the bottom panel of Fig. 3. Solid curves with error bars show the mean size and the standard error on the mean size. The scaled size–mass relations overlap with each other for the *LowZ* and *MidZ* samples. At $\sim 10^{11} M_{\odot}$, the scaled size of *HighZ* is the same as those for the *LowZ* and *MidZ*. This implies that most of the change in the amplitude of the relation between these samples can be explained by the evolution of the scale of dark matter haloes in which their stars form. The rescaled sizes are systematically lower for the *HighZ* sample (although the statistics are poor; the relations are in marginal agreement taking into account the error on the mean values).

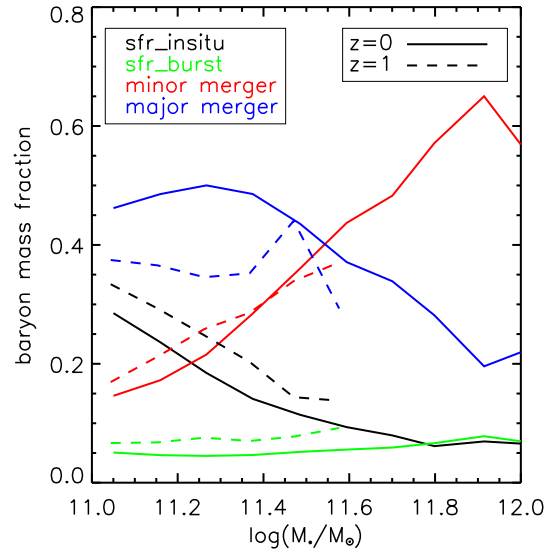


Figure 5. Stellar mass growth via different mechanisms as a function of stellar mass. Solid and dashed curves are for the *LowZ* and the *MidZ*, respectively. Black, green, red and blue curves are for the growth via in situ star formation, starburst, minor and major mergers, respectively.

4 FORMATION AND EVOLUTION OF ETGS

The last section demonstrated that evolution in the characteristic star formation time of galaxies classified as ETGs largely determines the amplitude of the ETG size–mass relation at different redshifts. In this section we explore the drivers of evolution in this relation, namely changes in the sizes and masses of galaxies over time.

4.1 Formation of ETGs

In Fig. 5 we sum the fractional contribution of in situ star formation, starbursts, minor and major mergers to mass growth along the main branch of the galaxy merger tree, for *LowZ* (solid) and *MidZ* (dashed) samples. This is done for every galaxy in each sample in bins of stellar mass at $z = 0$; we then plot the median contribution for each mass bin. Among ‘in situ’ star formation processes, we separate accreted stars formed in merger-induced starbursts (black lines) from stars formed in quiescent discs (green). We separate accreted stars according to the mass ratio of their progenitor, using the minor/major merger criterion (red/blue respectively).

The contribution from mergers dominates the growth in stellar mass at all masses. For the *LowZ* sample, below $3 \times 10^{11} M_{\odot}$, major mergers contribute a larger fraction of mass than minor mergers, while at higher masses, minor mergers dominate. The contribution from minor mergers increases with increasing stellar mass, while contribution from major mergers decreases. The *MidZ* sample does not include galaxies much beyond this transition mass; at lower masses the same trends are apparent, although major mergers become slightly less important relative to quiescent in situ star formation. In situ formation accounts for 35 and 40 per cent of the mass in the *LowZ* and *MidZ* samples, respectively, at low masses, and this contribution decreases with increasing galaxy mass. This limited contribution is not surprising in the context of the ETG selection, which, in the model, isolates objects that are dominated by massive spheroids and/or low star formation rates. The contribution from starbursts is only 5 and 7 per cent for the *LowZ* and *MidZ* samples, respectively, over all masses shown. This agrees with previous

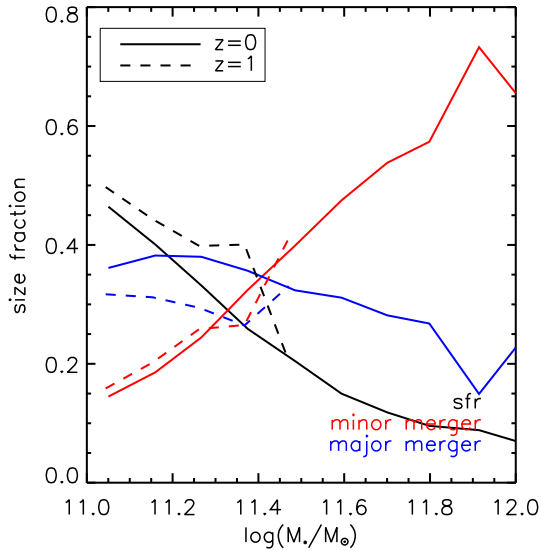


Figure 6. The growth of effective radius through different mechanisms as a function of stellar mass. All curves show median values. Black, red and blue curves are contributions from in situ star formation, minor and major mergers, respectively. Solid and dashed lines show the results of ETGs at redshift $z = 0$ and ~ 1 .

findings that most mergers that ETGs have experienced were gas poor (Hopkins et al. 2009; Naab et al. 2009; Oser et al. 2012). This is reassuring, because in this regime equation (6) is a reasonable approximation to size growth during mergers (Cole et al. 2000).

In Fig. 6 we compare the contribution of each of these galaxy-building processes to the change in galaxy size. In the model galaxy mass always increases, but the net change in size for individual galaxies can, in principle, be negative. The average change for galaxies in our ETG samples is positive, however. We combine the contribution of major or minor merger and the starburst it triggers and treat them together. Disc instability has neglected effect on size since typically only 3 per cent of the final bulge mass is involved.

The relative contributions of major and minor mergers to size change are very similar to their contribution to the stellar mass. The fraction of size growth attributable to major mergers decreases with final galaxy mass, while the fraction attributable to minor mergers increases. Interestingly, in situ star formation plays a more important role in the size growth of the *LowZ* sample compared to that in the mass growth, being responsible for to up to 50 per cent of the net increase in size of galaxies with final mass $\sim 10^{11} M_{\odot}$. The importance of in situ star formation decreases very rapidly with increasing stellar mass, as expected from its negligible contribution to the stellar mass in this regime. Mergers dominate the growth of the ETG size. We draw similar conclusions from the *MidZ* sample, in line with the relative differences in the contributions to the stellar mass growth between the two samples.

In Fig. 7 we show how four individual $z = 0$ ETGs in the model evolved, in order to understand better the average behaviour seen in previous figures. Each time one of these galaxies changes in size and mass, we plot a vector joining the initial and final positions in the size–mass plane. Mass increases monotonically, but size can increase or decrease. The colour of each vector corresponds to the mechanism responsible for the change. At low masses (high redshifts) our example trajectories are dominated by star formation (black), which contributes little to the final mass but induces rapid fluctuations in size. After $z = 2$ (dotted vertical lines), however, merging dominates. Consistent with the average behaviour, major

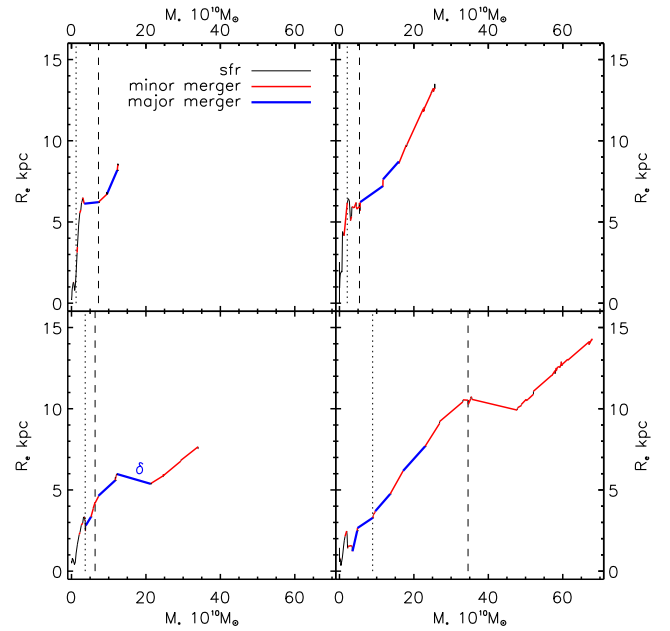


Figure 7. Examples of trajectories in the mass–size diagram for individual ETGs randomly selected from our sample. Line colours indicate the mode of growth in each size change (black: star formation; blue: major mergers; red: minor mergers). Vertical dotted and dashed lines indicate the masses corresponding to $z = 2$ and 1 , respectively. The blue δ marks a particular change which is discussed in the text.

mergers (blue) dominate in our lowest mass example and minor mergers (red) become more significant at higher final masses.

There are several notable features in the trajectories shown in Fig. 7. For example, there is no clear distinction in the typical slope (size change per unit additional mass) of the line segments corresponding to major and minor mergers. This is in part because the formula used to compute size change (equation 6) explicitly includes the mass ratio – it does not include a sharp boundary between the two classes of merger. In most cases the masses contributed by ‘minor’ mergers are almost as large as those contributed by major mergers, suggesting that they are not all that ‘minor’ and the distinction is somewhat artificial in this context. Another reason for the lack of a clear distinction is also related to the perhaps surprising result that mergers can have near-zero net size change and, in some cases, even make the remnant more compact than the primary progenitor. In the model this is not due to the dissipation of interaction energy by gas (which is not included) nor to the nuclear starburst (which contributes only a small amount of mass). Rather it is the result of mergers between a diffuse primary and a more compact secondary. Examination of equation (6) shows that this is readily achieved with mergers of moderate mass ratio. An example shown in Fig. 7, where the blue δ marks a case where size decreases after a major merger. Before the merger, the effective radius of the two progenitors are 5.9 and 1.7 kpc. The corresponding stellar masses are 12.2×10^{10} and $8.8 \times 10^{10} M_{\odot}$. After merger, the size of the remnant is 5.1 kpc.

4.2 Evolution of high-redshift ETGs

In the previous section we considered the contributions to size and mass growth since formation for all galaxies classified as ETGs at a particular epoch. This simulation also allows us to study the related (but not identical) question of how ETGs identified at a

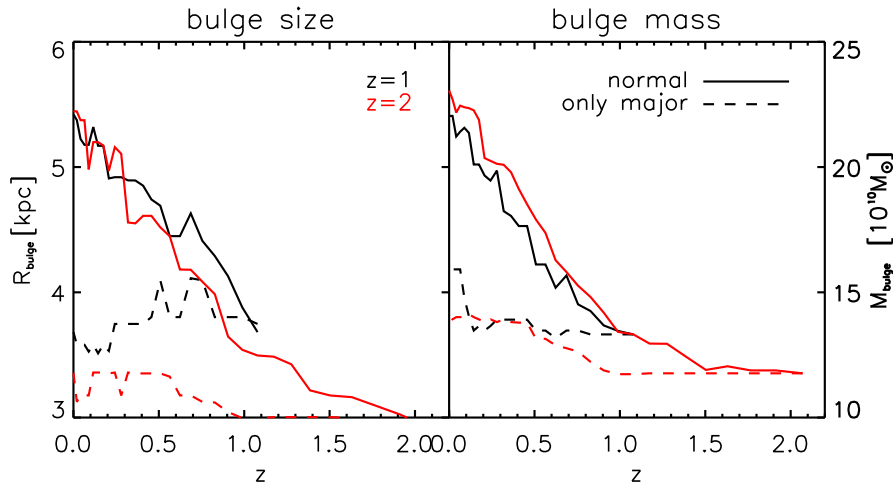


Figure 8. Median bulge half-mass radius (left) and median bulge mass (right) as a function of redshift. Black and red curves correspond to our *MidZ* and *HighZ* samples, respectively. Solid lines show the contributions of all mergers (including associated starbursts) and dashed lines the contributions from major mergers alone.

particular epoch subsequently evolve. Many authors have considered this question. Cenarro & Trujillo (2009) found the velocity dispersion of ETGs barely evolved since redshift $z \sim 2$ and thus concluded that minor mergers are responsible for the growth in size. Using hydrodynamical simulations, Naab et al. (2009) and Oser et al. (2012) also found that minor mergers are the main cause of ETG size evolution. Here we examine the causes of size growth in the *HighZ* and *MidZ* samples drawn from the semi-analytical galaxy formation model.

Fig. 8 shows how the average size and mass of *HighZ* ETGs (red solid lines) and *MidZ* ETGs (black solid lines) evolve to lower redshift. As these galaxies may regrow discs, we consider only the bulge component. The evolution of the *MidZ* sample more or less tracks that of *HighZ* ETGs, even though most of the *MidZ* galaxies were not ETGs at $z \sim 2$. We see that the median bulge mass of *HighZ* ETGs increases by a factor of 2 and the median size increases by a factor of 1.9. The fractional changes in the *MidZ* sample are similar (1.7 in mass and 1.5 in size).

We then switch off minor mergers and disc instabilities after the redshift of selection: stars accreted from satellites during minor mergers are added to the disc rather than the bulge, as are stars formed in bursts associated with these mergers. The resulting size and mass growth is considerably smaller in this case (dashed curves); a factor of 1.2 in mass and 1.1 in size between $z \sim 2$ and 0. Major mergers are therefore only responsible for weak size evolution from $z = 2$; from $z = 1$ they make almost no net contribution to mass growth and even appear to slightly decrease the average size. Clearly, the growth of $z \sim 2$ ETGs in the model is driven by minor mergers, in line with previous findings from semi-analytic models (De Lucia & Blaizot 2007) and hydrodynamical simulations (Naab et al. 2009; Oser et al. 2012).

5 CONCLUSION

We use an up-to-date semi-analytic galaxy formation model (Guo et al. 2011) to study the size evolution of massive ETGs. We find that the typical half-light radius of model ETGs selected at $z = 0$ is a factor of 1.8 larger than that of galaxies selected in the same way at $z = 2$. This finding is broadly consistent with several recent observational results.

This increase in the typical size of the ETG population can be attributed to two factors related to the fact that different galaxy populations are selected by our fiducial ETG criteria at different redshifts (the abundance of ETGs defined by these criteria increases by two orders of magnitude between $z = 2$ and 0, so the majority of present-day ETGs cannot have been ETGs at higher redshift).

First, since these criteria do not impose an upper limit on stellar mass, evolution in the shape of the high-mass end of the ETG stellar mass function results in an increasingly large fraction of extremely massive and extended galaxies entering the ETG sample at lower redshifts. However, the median mass increases only by 25 per cent as a result of this effect, which is far from enough to account for the factor of 1.8 difference in the typical ETG size.

The second and more significant factor is a ‘real’ difference in the size–stellar mass relation of galaxies selected as ETGs at these different redshifts. We find that the Guo et al. (2011) model reproduces the slope and amplitude of the observed relation from $z \sim 2$ to 0 at the 1σ level. This motivates us to explore the origin of this evolution in the model. In the standard Λ CDM cosmology, dark matter haloes forming at earlier times are more concentrated. Our model for the initial sizes of gas discs based on the conservation of angular momentum translates this into a smaller average scale for galaxies formed at high redshift. We can demonstrate this by scaling the radii of ETGs according to the time when half of their stars formed; with this rescaling, ETG samples selected at different redshifts lie on roughly the same median size–mass relation. Hence the increase in amplitude of the relation at lower redshift is mostly explained by increasing numbers of more recently formed galaxies entering the ETG sample.

Mergers, stellar accretion and further in situ star formation during the low-redshift evolution of ETGs preserve this formation time dependence, to a greater or lesser extent. Mergers always dominate over star formation in the late-time mass and size growth of ETGs. Minor mergers play a more important role only for ETGs at $M_* > 3 \times 10^{11} M_\odot$. Merger-driven starbursts contribute only about 5 per cent, in line with the fact that most mergers are gas poor after $z \sim 1$. In situ star formation contributes more to size growth than it does to stellar mass growth, though in both cases, it is subdominant compared to mergers. We find that ETGs selected at high redshifts grow mainly via minor mergers to their present-day configuration.

Bulge mass and size grow by a factor of 2.0 and 1.9 from $z \sim 2$ to 0, respectively. Our study of individual galaxies in the model highlights the fact that individual mergers and star formation events can also decrease their size.

We note that the model used here does not take into account the gravitational energy dissipated by gas processes during mergers, which could reduce the size of the remnant. This is most important at higher redshift where gas-rich mergers are more common, reflected in the relatively larger size of the model predictions when compared to the data at $z \sim 2$ (Shankar et al. 2013; Porter et al. 2014).

Most ETGs identified at high redshift evolve into central galaxies at the present day (although most central galaxies today were *not* ETGs at high redshift). It is interesting to study the progenitors of ETGs identified at different redshifts and their relation with other high-redshift populations, such as extremely red galaxies and Lyman break galaxies. This will be done in a companion work in the near future (Xie et al., in preparation).

ACKNOWLEDGEMENTS

We acknowledge support from NSFC grants (Nos 11143005, 11133003 and 11303033) and the Strategic Priority Research Program ‘The Emergence of Cosmological Structure’ of the Chinese Academy of Sciences (No. XDB09000000). QG acknowledges a Royal Society Newton International Fellowship. RL acknowledges the support from Youth Innovation Promotion Association of CAS. LG acknowledges the MPG partner Group family, and an STFC Advanced Fellowship, as well as the hospitality of the Institute for Computational Cosmology at Durham University.

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